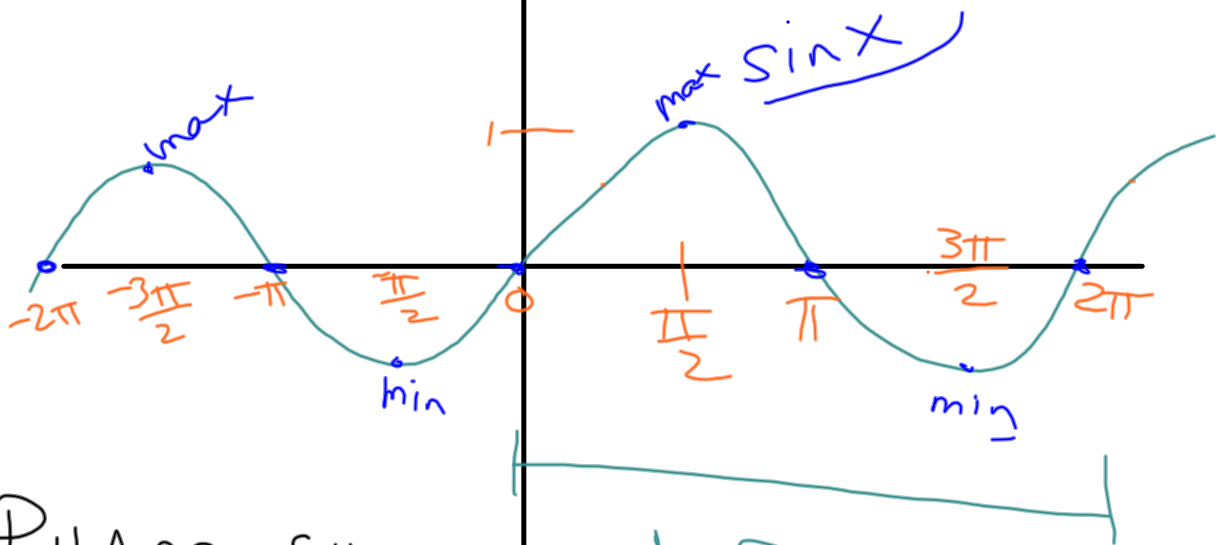


7.1

$$\text{AMPLITUDE} = \frac{1}{2} \text{RANGE}$$



PHASE SHIFT
secret code word for
horizontal shift

1 PERIOD

FREQUENCY

= how many periods
in 2π

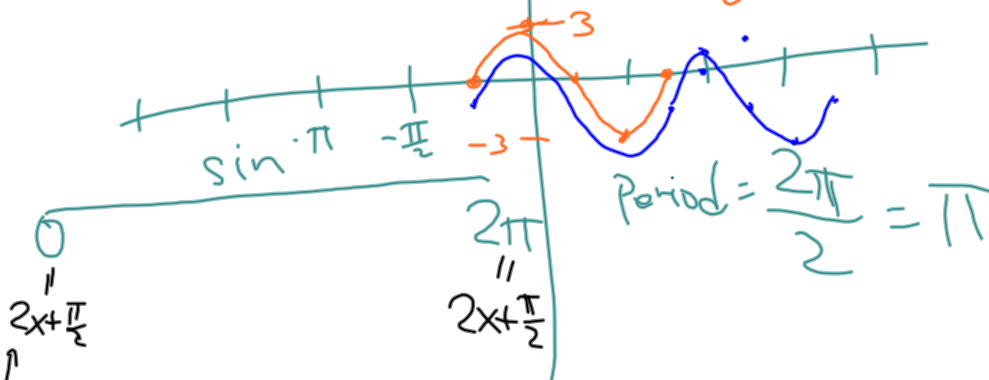
$$3 \sin\left(2x + \frac{\pi}{2}\right) - 1$$

amplitude

frequency

vert shift

hpr shift



$$\begin{aligned} 2x + \frac{\pi}{2} &= 0 \\ 2x &= -\frac{\pi}{2} \\ x &= -\frac{\pi}{4} \end{aligned}$$

$$\begin{aligned} 2x + \frac{\pi}{2} &= 2\pi \\ 2x &= 2\pi - \frac{\pi}{2} = \frac{3\pi}{2} \\ x &= \frac{3\pi}{4} \end{aligned}$$

$$\text{Period} = \frac{3\pi}{4} - \left(-\frac{\pi}{4}\right) = \frac{3\pi}{4} + \frac{\pi}{4} = \frac{4\pi}{4} = \pi$$

Division Algorithm Theorem

$$P(x) = Q(x) D(x) + R(x)$$

$$P(x) = Q(x)(x-c) + R(x)$$

$$P(c) = Q(c)(c-c) + R(c)$$

$$4.1 \bigg|_{33} f(x) = 3x^4 - 6x^3 + 2x - 1$$

Find remainder when $f(x)$ is divided by $x+1$

but don't use division.

$$f(x) = Q(x) \cdot (x+1) + R(x)$$

select $x = -1$ divisor

$$f(-1) = R(-1)$$

$$f(-1) = 3(-1)^4 - 6(-1)^3 + 2(-1) - 1$$

$$= +3 + 6 - 2 - 1 = 6$$

degree of $R(x)$
LESS THAN
degree(divisor)

$$\begin{array}{r} \cancel{3x^3 - 9x^2 + 9x - 7} \\ x+1 \overline{) 3x^4 - 6x^3 + 0x^2 + 2x - 1} \\ \underline{-(3x^4 + 3x^3)} \end{array}$$

$$\begin{array}{r} -9x^3 + 0x^2 + 2x - 1 \\ \underline{-(-9x^3 - 9x^2)} \end{array}$$

$$\begin{array}{r} 9x^2 + 2x - 1 \\ \underline{-(9x^2 + 9x)} \end{array}$$

$$\begin{array}{r} -7x - 1 \\ \underline{-(-7x - 7)} \end{array}$$

$$+6$$

4.1/21

$5x^4 + 5x^2 + 5$ divide by $x^2 - x + 1$

$$\begin{array}{r} x^2 - x + 1 \overline{) 5x^4 + 0x^3 + 5x^2 + 0x + 5} \\ \underline{-(5x^4 - 5x^3 + 5x^2)} \end{array}$$

$$\frac{5x^4}{x^2} = 5(x^{4-2})$$

$$= 5x^2$$

$$\begin{array}{r} 5x^3 + 0x^2 + 0x + 5 \\ \underline{-(5x^3 - 5x^2 + 5x)} \end{array}$$

$$\begin{array}{r} 5x^2 - 5x + 5 \\ \underline{-(5x^2 - 5x + 5)} \end{array}$$

$$5x^4 + 5x^2 + 5 = (x^2 - x + 1)(5x^2 + 5x + 5) + 0$$

$$x^2 - x + 1 = 0$$

$$\text{QF: } x = \frac{+1 \pm \sqrt{1 - 4(1)(1)}}{2}$$

$$x + 1 = 0$$

$$\text{root: } x = -1$$

$$-1 \mid 3 \quad -6 \quad 0 \quad 2 \quad -1$$

